

LISTA 4: DERIVADAS, PARTE I

Exercício 1. Calcule as derivadas, utilizando a def. da derivada:

1. $f(x) = 2x^2 - 16x + 35$ (Resp: $4x - 16$)
2. $g(t) = \frac{t}{t+1}$ (Resp: $(\frac{1}{t+1})^2$)
3. $R(z) = \sqrt{5z - 8}$ (Resp: $\frac{5}{2\sqrt{5z - 8}}$)

Exercício 2. Determine a reta tangente para:

1. $R(z) = \sqrt{5z - 8}$ no ponto $z = 3$ (Resp: $y = \sqrt{7} + \frac{5}{2\sqrt{7}}(z - 3)$)
2. $f(x) = 4x - 8\sqrt{x}$ no ponto $x = 16$. (Resp: $y = 32 + 3.(x - 16)$)

Exercício 3. Calcule as derivadas (pode utilizar todas as leis das derivadas...):

- a) $f(x) = 15x^{100} - 3x^{12} + 5x - 46$ (Resp: $1500x^{99} - 36x^{11} + 5$)
- b) $g(t) = 2t^6 - 7t^{-6}$ (Resp: $12t^5 - 42t^{-7}$)
- c) $y = 8z^3 - \frac{1}{3z^5} + z - 23$ (Resp: $y' = 24z^2 + \frac{5}{3}z^{-6} + 1$)
- d) $T(x) = \sqrt{x} + 9\sqrt[3]{x^7} - \frac{2}{x^{2/5}}$ (Resp: $T'(x) = \frac{1}{2}x^{-1/2} + \frac{63}{3}x^{4/3} + \frac{4}{5}x^{-7/5}$)
- e) $y = x^{2/3} \cdot (2x - x^2)$ (Resp: $y' = \frac{10}{3}x^{2/3} - \frac{8}{3}x^{5/3}$)
- f) $h(t) = \frac{2t^5 + t^2 - 5}{t^2}$ (Resp: $6t^2 + 10t^{-3}$)
- g) $h(x) = \frac{4\sqrt{x}}{x^2 - 2}$ (Resp: $\frac{-6x^{3/2} - 4x^{1/2}}{(x^2 - 2)^2}$)

Exercício 4. Calcule os limites (pode utilizar derivadas!)

- a) $\lim_{x \rightarrow 4} \frac{\sin(x-4)}{x-4}$ (Resp: $= 1$)
- b) $\lim_{z \rightarrow 0} \frac{\cos(2z) - 1}{z}$ (Resp: $= 0$)

Exercício 5. Calcule as derivadas:

- a) $P(t) = \frac{\sin t}{3 - 2 \cos t}$ (Resp: $P'(t) = \frac{3\cos(t) - 2}{(3 - 2\cos(t))^2}$)
- b) $R(w) = 4^w - 5\log_9 w$ (Resp: $R'(w) = 4^w \ln(4) - \frac{5}{w \ln 9}$)
- c) $f(x) = 3e^x + 10x^3 \ln x$ (Resp: $3e^x + 30x^2 \ln(x) + 10x^2$)

$$d) \ y = \frac{5e^x}{3e^x + 1} \ (\text{Resp: } \frac{5e^x}{(3e^x + 1)^2})$$

$$e) \ f(t) = 4 \cos^{-1} t - 10 \operatorname{tg}^{-1} t \ (\text{Resp: } = -\frac{4}{\sqrt{1-t^2}} - \frac{10}{1+t^2})$$

$$f) \ y = \sqrt{z} \cdot \operatorname{sen}^{-1} z \ (\text{Resp: } = \frac{1}{2} z^{-1/2} \operatorname{sen}^{-1}(z) + \frac{\sqrt{z}}{\sqrt{1-z^2}})$$

Exercício 6. Determine as derivadas, com a regra da cadeia:

$$a) \ f(x) = \operatorname{sen}(3x^2 + x) \ (\text{Resp: } = (6x + 1)\cos(3x^2 + x))$$

$$b) \ h(w) = e^{w^4 - 3w^2 + 9} \ (\text{Resp: } (4w^3 - 6w)e^{w^4 - 3w^2 + 9})$$

$$c) \ g(x) = \ln(x^{-4} + x^4) \ (\text{Resp: } = \frac{-4x^{-5} + 4x^3}{x^{-4} + x^4})$$

$$d) \ f(x) = e^{g(x)} \ (\text{Resp: } = e^{g(x)} \cdot g'(x))$$

$$e) \ f(x) = \ln(g(x)) \ (\text{Resp: } = \frac{g'(x)}{g(x)})$$

$$f) \ y = \frac{(x^3 + 4)^5}{(1 - 2x^2)^3} \ (\text{Resp: } = \frac{3x(x^3 + 4)^4(5x - 6x^3 + 16)}{(1 - 2x^2)^4})$$

$$g) \ f(x) = \sqrt{2y + (3y + 4y^2)^3}$$

$$\text{Resp: } = \frac{1}{2}(2y + (3y + 4y^2)^3)^{-1/2}(2 + (9 + 24y)(3y + 4y^2)^2)$$